

「微分積分問題集 6 章 6.1」正誤表 (2016 年 2 月 22 日現在)

[illegible]

第6章

6.1節 1 (1) $\frac{166}{3}$ (2) $\frac{19}{12}$

2 (1) $\int_0^2 \left\{ \int_0^3 (x^2 + y^2) dy \right\} dx$, 26

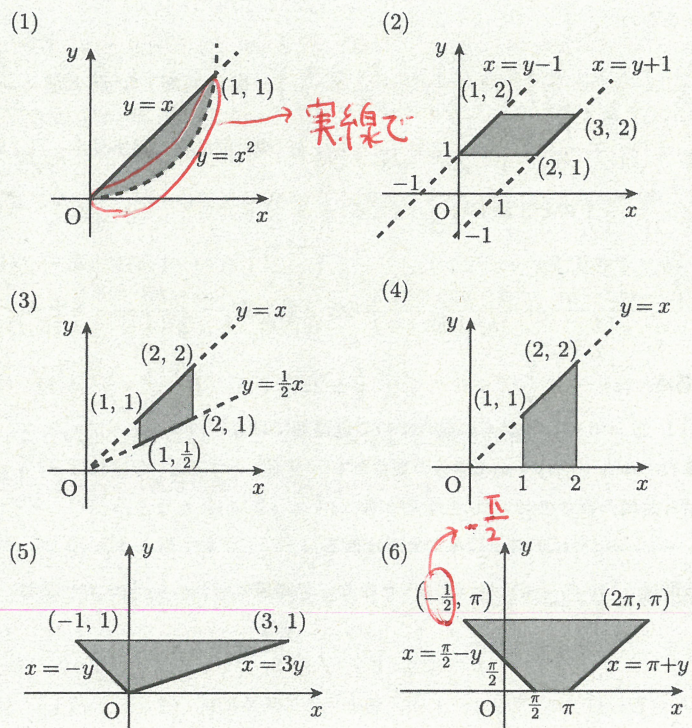
(2) $\int_0^3 \left\{ \int_0^2 (x^2 + y^2) dx \right\} dy$, 26

3 (1) 2 (2) $-\frac{103}{12}$ (3) $4(e-1)$ (4) $\frac{8}{15}(2\sqrt{2}-1)$ (5) 2

4 $\iint_D \sqrt{a^2 - x^2 - y^2} dx dy$, $D = \{(x, y) \mid x^2 + y^2 \leq a^2\}$

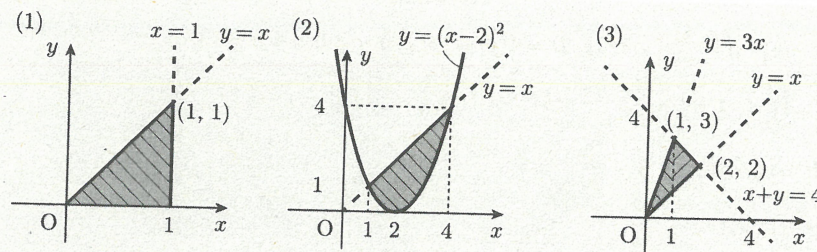
5 (1) $\frac{13}{60}$ (2) 9 (3) $\frac{3}{2} \log 2$ (4) $\frac{\pi}{4} \log 2$ (5) $\frac{16}{3}$

(6) -2 図は以下に示す.



6 $L=1, M=-2x+2$

7 (1) $\frac{1}{6}$ (2) $\frac{45}{4}$ (3) 2 図は以下に示す.

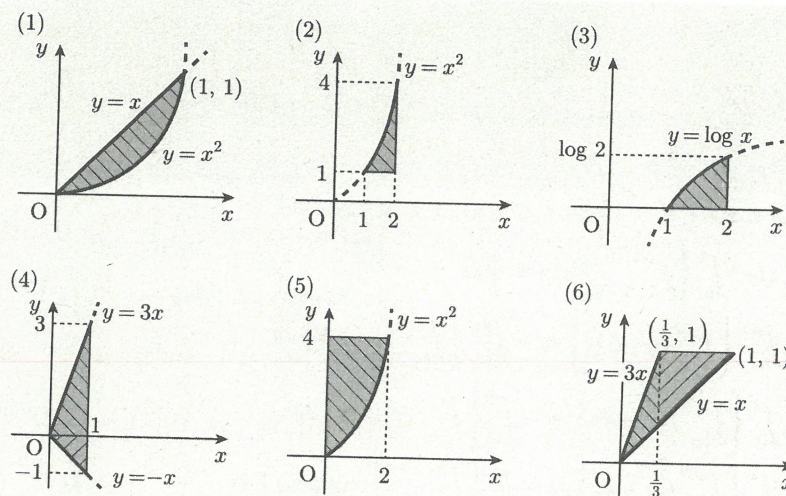


8 (1) $\int_0^1 \left\{ \int_y^{\sqrt{y}} f(x, y) dx \right\} dy$ (2) $\int_1^4 \left\{ \int_{\sqrt{y}}^2 f(x, y) dx \right\} dy$

(3) $\int_0^{\log 2} \left\{ \int_{e^y}^2 f(x, y) dx \right\} dy$ (4) $\int_{-1}^0 \left\{ \int_{-y}^1 f(x, y) dx \right\} dy + \int_0^3 \left\{ \int_{\frac{y}{3}}^1 f(x, y) dx \right\} dy$

(5) $\int_0^2 \left\{ \int_{x^2}^4 f(x, y) dy \right\} dx$ (6) $\int_0^{\frac{1}{3}} \left\{ \int_x^{3x} f(x, y) dy \right\} dx + \int_{\frac{1}{3}}^1 \left\{ \int_x^1 f(x, y) dy \right\} dx$

図は以下に示す.



$$9 \quad (1) \int_0^1 \left\{ \int_0^y e^{-\frac{1}{2}y^2} dx \right\} dy, 1 - \frac{1}{\sqrt{e}} \quad (2) \int_0^1 \left\{ \int_{y^2}^y e^{\frac{3x}{y}} dx \right\} dy, \frac{1}{54}(5e^3 - 2)$$

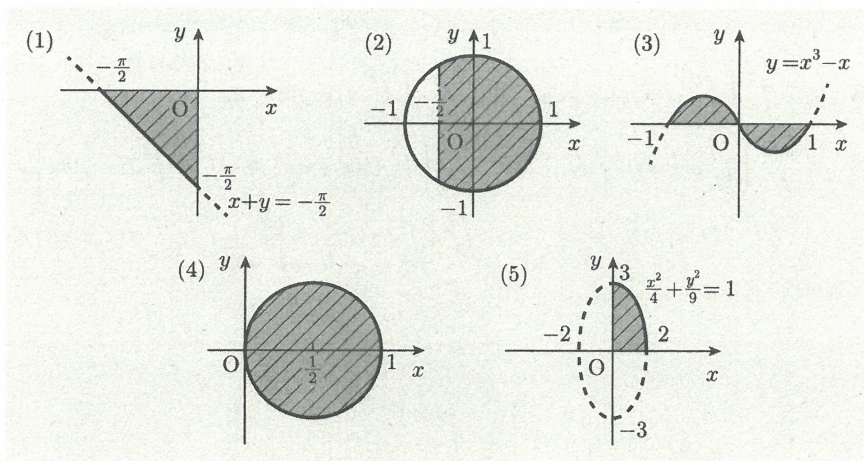
$$10 \quad a + 2b + 2c \quad \left(\text{ヒント: } \lim_{m \rightarrow \infty} \sum_{i=1}^m \sum_{j=1}^n \left(a \frac{i}{m} + b \frac{2j}{n} + c \right) \frac{1}{m} \frac{2}{n} \right)$$

$$11 \quad (1) \iint_D f(x, y) dx dy, D = \{(x, y) \mid x \geq 0, y \geq 0, x + y \leq 1\}$$

$$(2) \iint_D (-1 + \sqrt{4 - x^2 - y^2}) dx dy, D = \{(x, y) \mid x^2 + y^2 \leq 3\}$$

$$12 \quad (1) -1 \quad (2) \frac{\sqrt{3}}{2} \quad (3) \frac{1}{6} \quad (4) \frac{8}{15} \quad (5) \frac{9}{2}$$

図は以下に示す。



$$13 \quad (1) A = 2, B = \sqrt{x}$$

$$(2) A = x + 1, B = -\frac{1}{2}x + 1, C = y - 1, D = -2y + 2$$

$$14 \quad (1) \int_0^1 \left\{ \int_{-\sqrt{1-y}}^{\sqrt{1-y}} f(x, y) dx \right\} dy$$

$$(2) \int_0^{pa} \left\{ \int_{\frac{1}{q}y}^{\frac{1}{p}y} f(x, y) dx \right\} dy + \int_{pa}^{qa} \left\{ \int_{\frac{1}{q}y}^a f(x, y) dx \right\} dy$$

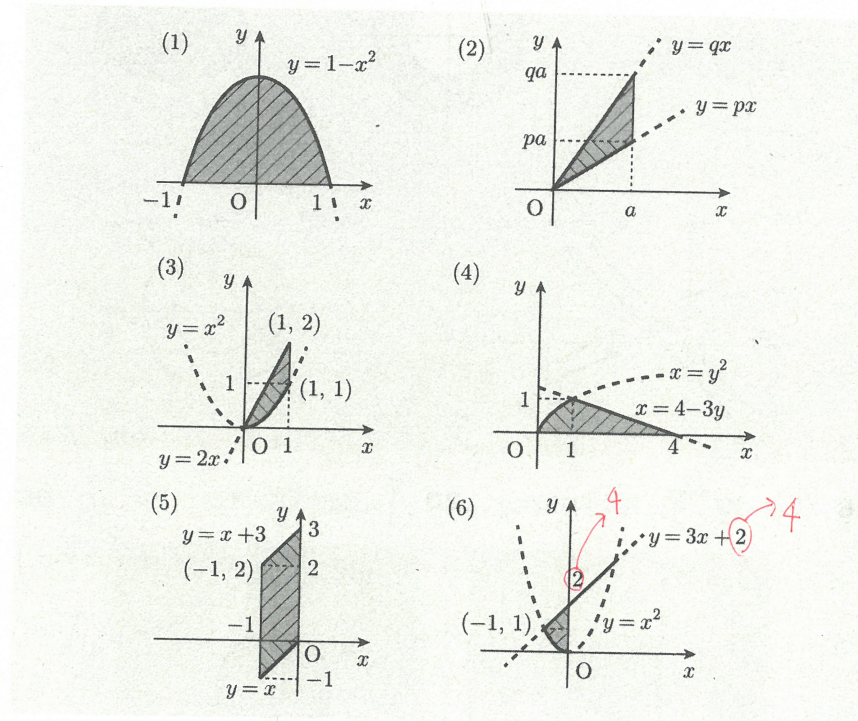
$$(3) \int_0^1 \left\{ \int_{\frac{1}{2}y}^{\sqrt{y}} f(x, y) dx \right\} dy + \int_1^2 \left\{ \int_{\frac{1}{2}y}^1 f(x, y) dx \right\} dy$$

$$(4) \int_0^1 \left\{ \int_0^{\sqrt{x}} f(x, y) dy \right\} dx + \int_1^4 \left\{ \int_0^{\frac{1}{3}(-x+4)} f(x, y) dy \right\} dx$$

$$(5) \int_{-1}^0 \left\{ \int_{-1}^y f(x, y) dx \right\} dy + \int_0^2 \left\{ \int_{-1}^0 f(x, y) dx \right\} dy + \int_2^3 \left\{ \int_{y-3}^0 f(x, y) dx \right\} dy$$

$$(6) \int_0^1 \left\{ \int_{-\sqrt{y}}^0 f(x, y) dx \right\} dy + \int_1^4 \left\{ \int_{\frac{1}{3}(y-2)}^0 f(x, y) dx \right\} dy$$

図は以下に示す。



$$15 \quad (1) \int_0^{\sqrt{\pi}} \left\{ \int_0^y y^2 \cos(xy - y^2) dx \right\} dy, 1$$

$$(2) \int_0^1 \left\{ \int_0^x \frac{1}{1+x^2} dy \right\} dx, \frac{1}{2} \log 2$$

$$16 \quad (1), (2) \text{ 証明略 } \left(\text{ヒント: 積分順序を変更することにより証明する.} \right)$$

$$(1) \text{ (左辺) } = \int_0^a \left\{ \int_x^a (y-x)^n f(x) dy \right\} dx$$

$$(2) \text{ (左辺) } = \int_0^a \left\{ \int_{a-y}^a (a-x)^n f(y) dx \right\} dy$$

「微分積分問題集」6章6.4節 正誤表 (2016年 2月 1日)

頁	場所	誤	正
p.132	上から3行目	$z = 2x$	$z = 2$
p.179	上から10行目	8	4π
p.179	上から10行目	$2 \int_0^1 \left\{ \int_0^{2x} \frac{2}{\sqrt{1-x^2}} dz \right\} dx$	$2 \int_0^1 \left\{ \int_0^2 \frac{2}{\sqrt{1-x^2}} dz \right\} dx$